## Transformations Review

1. If $(2,3)$ is a point on the graph of $y=f(x)$, what point must be on the graph of $y=3 f\left(\frac{1}{4} x\right)$ ?
2. Determine one possible restriction for the domain of $y=(x+3)^{2}-4$ so that its inverse is a function.
3. The range of the graph $y=f(x)$ is $[-3,2]$. Explain why there is no effect on the range of the graph that is a result of the transformation $y=f(-x)$.
4. Given the graph of $f(x)$ below, sketch the graph of $y=-f(x)$.

5. Sketch the graph of $y=\sqrt{2 x-2}$.
6. Given $f(x)=2 x-6$, write the equation of $f^{-1}(x)$.
7. Describe the effects on the graph of $y=f(x)$ when asked for the graph of $y=f(x-3)+5$.
8. Given the graph of $y=f(x)$, describe the transformations necessary to obtain the graph of the function $y=f(2 x-6)$.
9. Given $f(x)=\{(-3,4),(2,7),(8,6)\}$, state the domain of the resulting function after $f(x)$ is reflected through the line $y=x$.
10. If the point $(3,-2)$ is on the graph of $y=f(x)$, what point must be on the graph of $y=2 f(x+1)$ ?
11. Given $f(x)=4-x$, verify that $f^{-1}(x)=f(x)$.
12. Sketch the graph of $y=\sqrt{x+1}-2$ and verify that the value of the $x$-intercept is the same as the solution to the equation $\sqrt{x+1}-2=0$.
13. Alex incorrectly explains to Rashid that the graph of $y=2 f(x)+5$ means you first move the graph of $y=f(x)$ up 5 units and then multiply the $y$ values by 2. Explain to Rashid the correct way to transform the graph.
14. Given the graph of $f(x)$ below, sketch the graph of $g(x)=f(x-2)+3$.

15. If the point $(4,-3)$ lies on the graph of $f(x)$, which point must lie on the graph of $2 f(2 x)$ ?
16. The graph of $y=\left(\frac{1}{2}\right)^{x}$ compared to the graph of $x=\left(\frac{1}{2}\right)^{y}$ is a $\qquad$ .
17. Given $f(x)=(x+1)^{2}$ for $x \leq-1$, write the equation of $y=f^{-1}(x)$.
18. Determine one possible restriction for the domain of $f(x)=(x-1)^{2}$ so that the inverse of $f(x)$ is a function.
19. The graph of $f(x)=x^{2}+4$ is reflected over the $x$-axis. Write the equation of the new function.
20. Given the graph of $y=f(x)$ below, sketch the graph of $y=2 f(x)-3$.

21. Given $f(x)=x^{2}-x+2$, write an equation that represents the graph of $f(x)$ shifted 3 units to the right.
22. What is the domain of the function $y=\sqrt{-4 x}$ ?
23. Given the graph of $f(x)$ contains the point $(-3,5)$, what point must be on the graph of $f(-x)$ ?
24. Sketch the graph of $y=-\sqrt{3(x+1)}$.
